

Electromagnetic Fields – Assignment 05

#	Student ID	Student Name	Grade (10)
-			

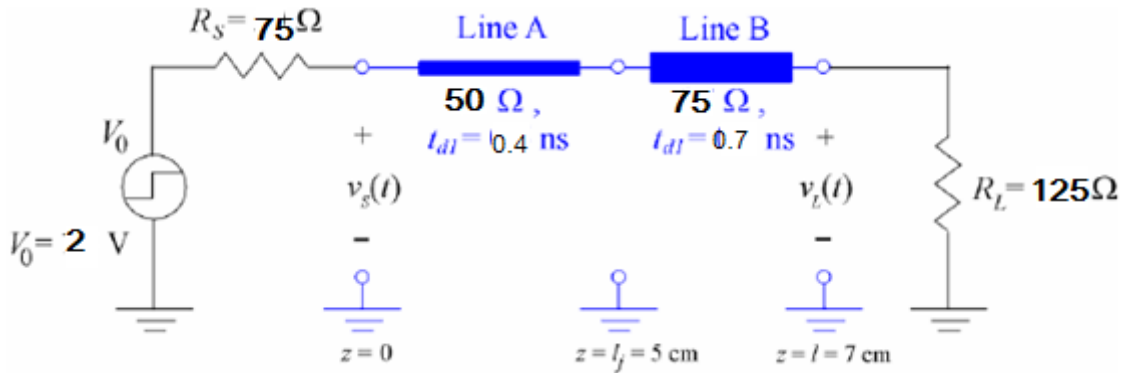
Delivery Date	
---------------	--

<p>١. يتم تسليم التمرين محلولا في خلال أسبوع من تاريخ التمرين، و يتم حذف درجتين من التمرين عن كل أسبوع تأخير ٢. يتم التسليم لمعيد المقرر مباشرة ٣. تتم أجابه التمرين في نفس ورق الأسئلة</p>

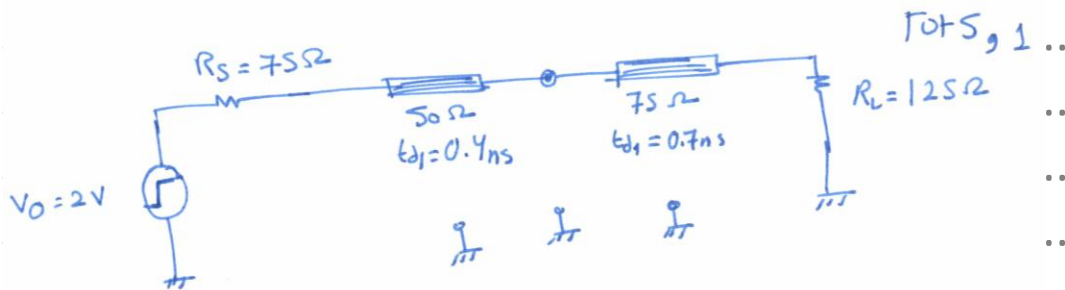


Q1

Consider a system shown in Fig. Find the terminal voltages $v_s(t)$, $v_L(t)$.



Sol
1



$$\Gamma_S = \frac{R_S - Z_A}{R_S + Z_A} = \frac{75 - 50}{75 + 50} = 0.2$$

$$\Gamma_{AB} = \frac{Z_B - Z_A}{Z_A + Z_B} = \frac{75 - 50}{75 + 50} = 0.2$$

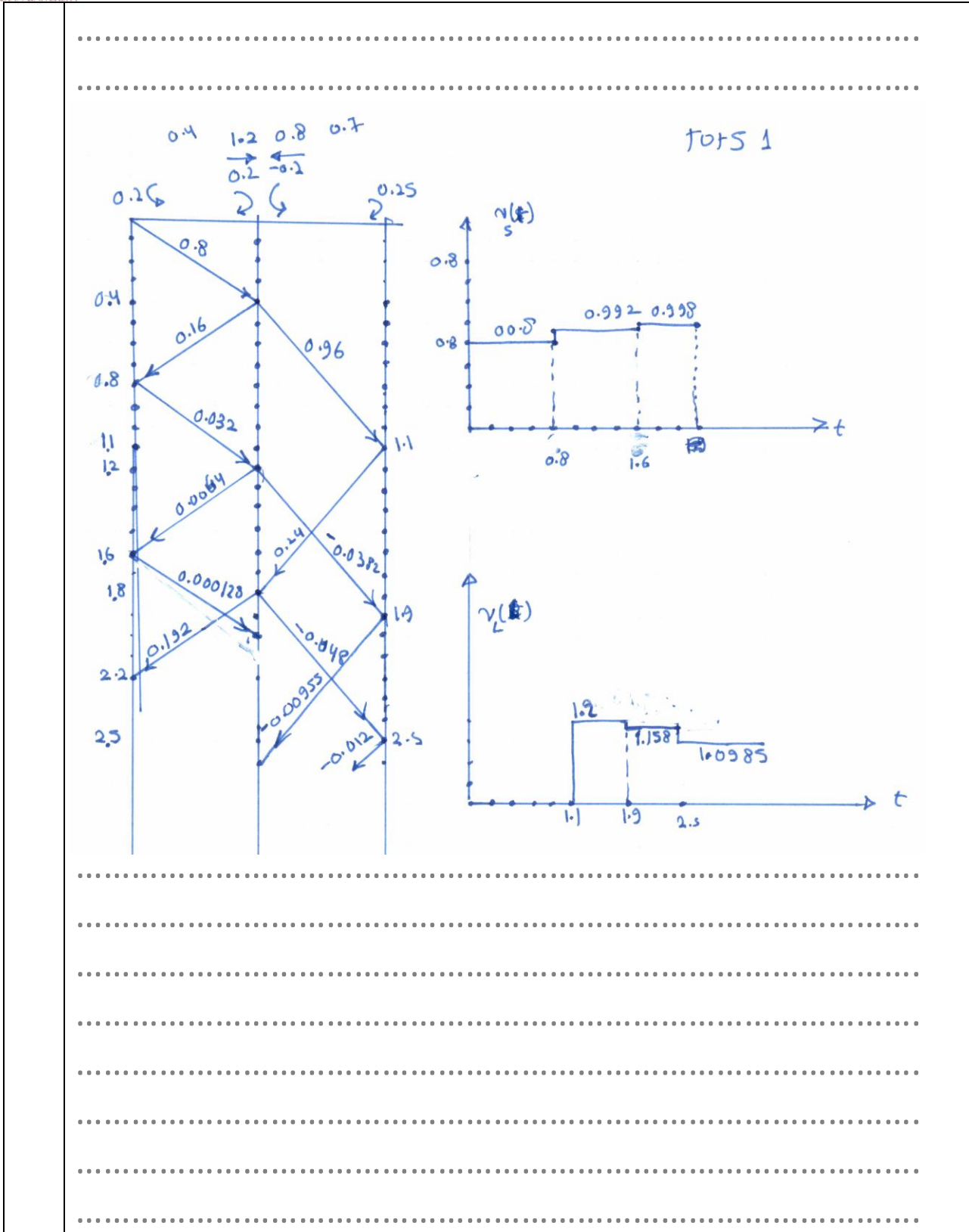
$$T_{AB} = 1 - \Gamma_{AB} = 0.8$$

$$\Gamma_{BA} = \frac{Z_A - Z_B}{Z_A + Z_B} = \frac{50 - 75}{50 + 75} = -0.2$$

$$T_{BA} = 0.8$$

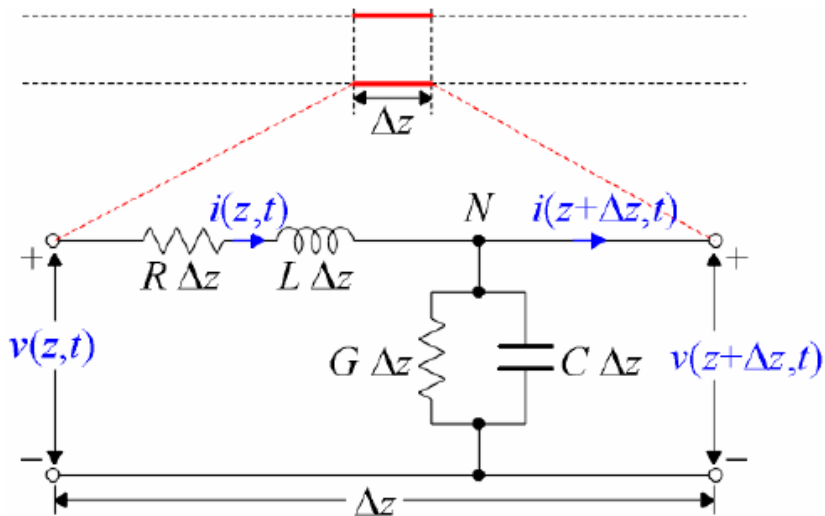
$$\Gamma_L = \frac{R_L - Z_B}{R_L + Z_B} = \frac{125 - 75}{125 + 75} = 0.25$$

$$V_{1A}^+ = V_0 \frac{Z_A}{Z_A + R_S} = 2 \times \frac{50}{50 + 75} = 0.8V$$



Q2

For a lossless transmission line we drives the following equation



Equivalent circuit of a real transmission line.

$$\frac{d}{dz} V(z) = -j\omega L \cdot I(z)$$

$$\frac{d}{dz} I(z) = -j\omega C \cdot V(z)$$

assuming that $R = 0, G = 0$

Please modify them if the line is lossy ($R \neq 0, G \neq 0$).

Sol 2

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....



we know that

$$\frac{\partial v(z,t)}{\partial z} = -L \frac{\partial i(z,t)}{\partial t} \Rightarrow \frac{d}{dz} V(z) = -j\omega L I(z) \rightarrow (1)$$

for a lossy TX

$$v(z,t) - v(z+\Delta z,t) = i(z,t)R\Delta z + L\Delta z \frac{\partial i(z,t)}{\partial t}$$

When $\Delta z \rightarrow 0$

$$\frac{\partial v(z,t)}{\partial z} = -i(z,t)R - L \frac{\partial i(z,t)}{\partial t} \rightarrow (2)$$

sub from 1

$$\frac{d}{dz} V(z) = -R I(z) - j\omega L I(z)$$

we know that

$$\frac{\partial i(z,t)}{\partial z} = -C \frac{\partial v(z,t)}{\partial t} \Rightarrow \frac{d}{dz} I(z) = -j\omega C V(z) \rightarrow (3)$$

for lossy TX

$$i(z,t) = i(z+\Delta z,t) + C\Delta z \frac{\partial v(z+\Delta z,t)}{\partial t} + G\Delta z v(z+\Delta z,t)$$

When $\Delta z \rightarrow 0$

$$\frac{\partial i(z,t)}{\partial z} = -v(z,t)G - C \frac{\partial v(z,t)}{\partial t} \rightarrow (4)$$

sub from 3

$$\frac{d}{dz} I(z) = -G V(z) - j\omega C V(z)$$